

Principles of Protein Structure and Conformational Space

Protein structure

1. Introduction

1. Amino acids
2. Peptide bond
3. Native conformation
4. Levels of structure (1,2,3)

2. Energy

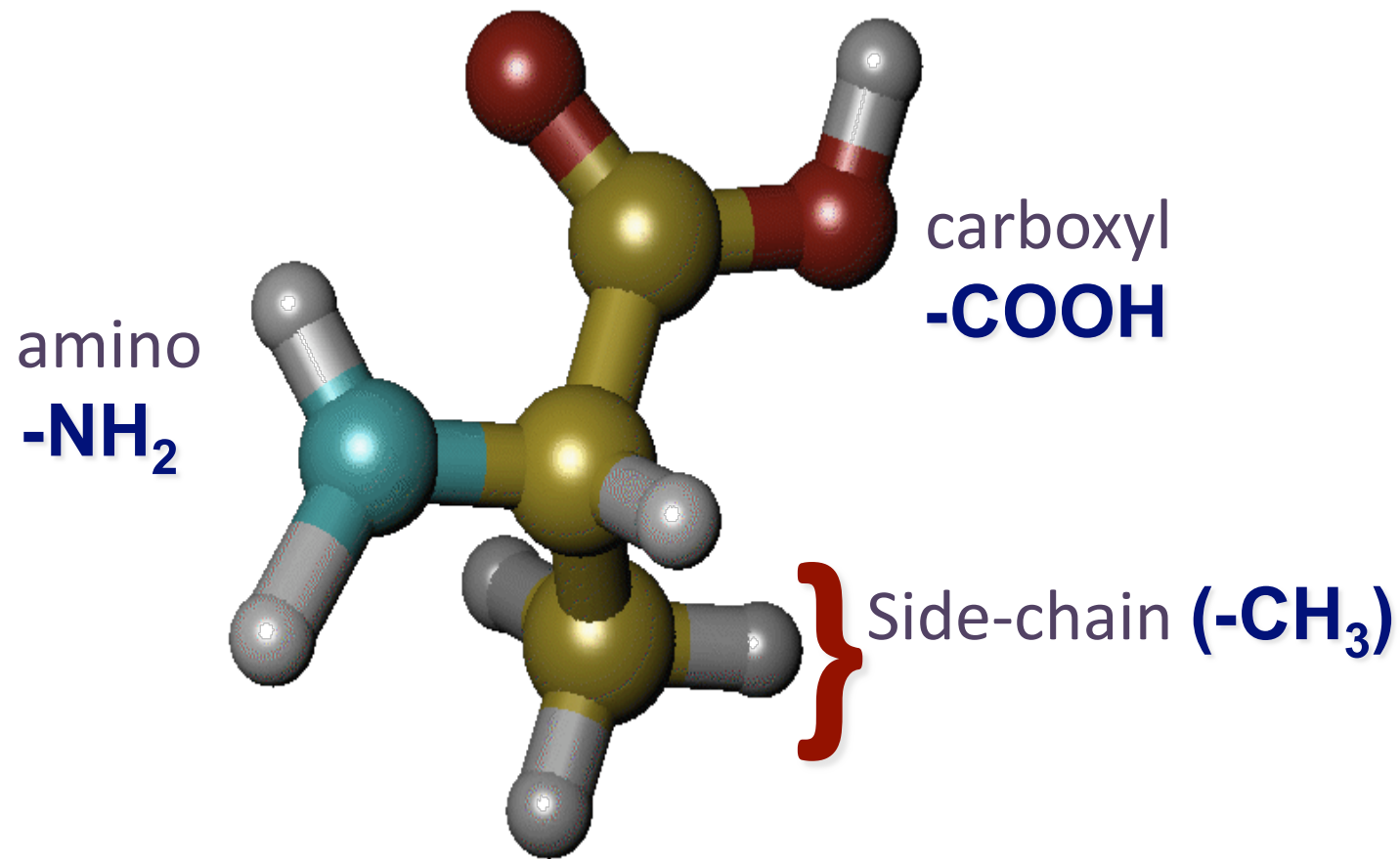
1. Bonding energy terms
2. Non-bonding terms

3. Secondary Structure

1. Strands
2. Helix
3. Ramachandran Plot
4. Aa propensities

1. Introduction

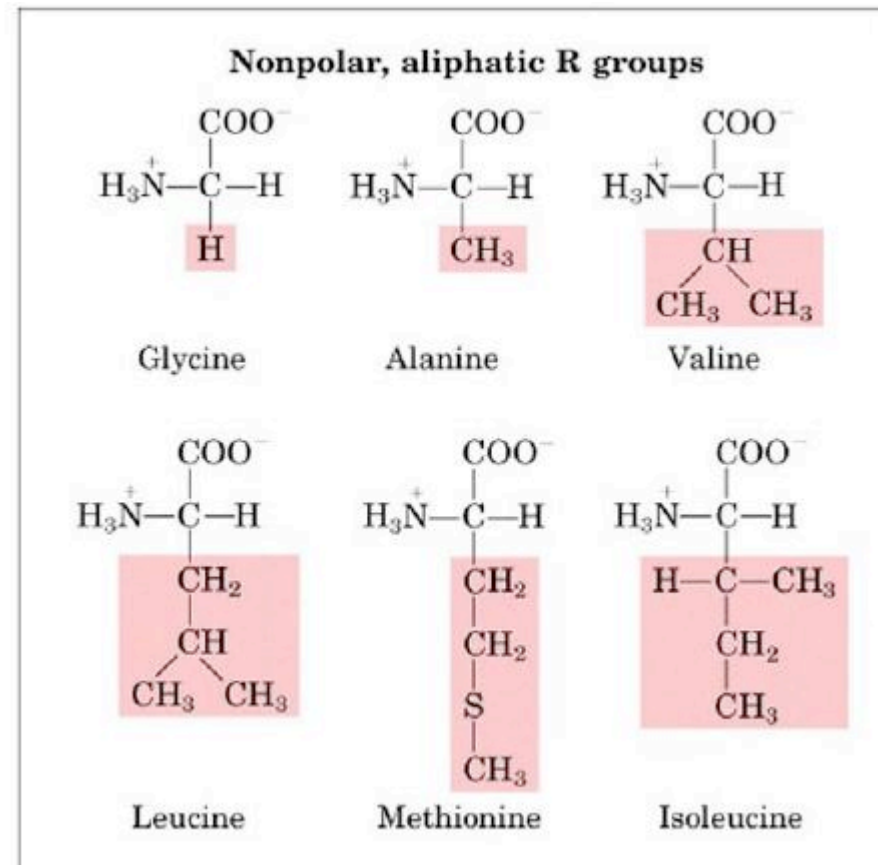
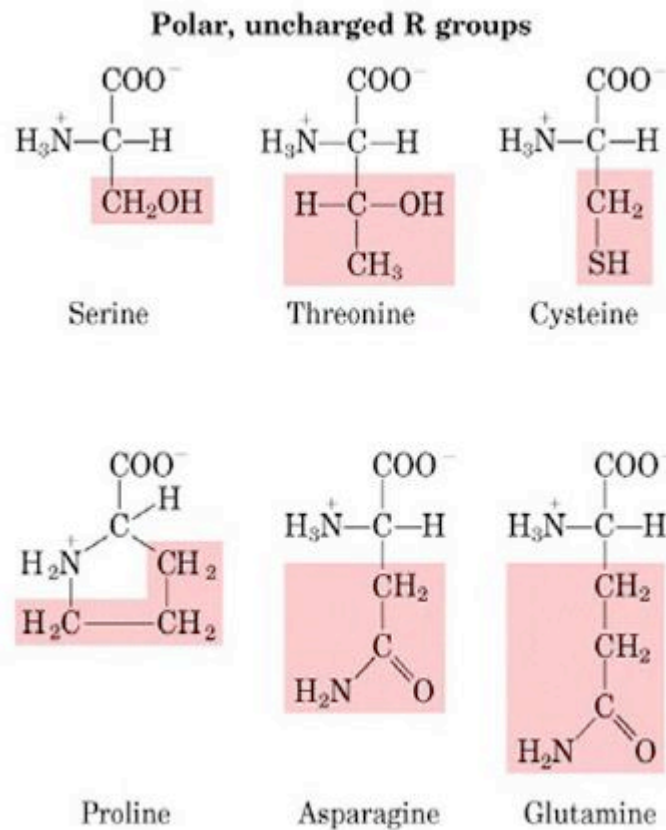
1. Amino Acids



Estereoisomer L

1. Introduction

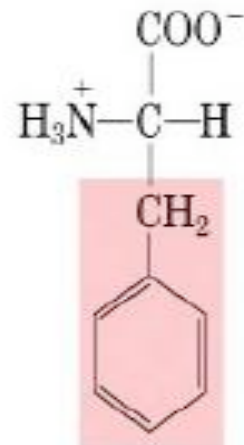
1. Amino Acids



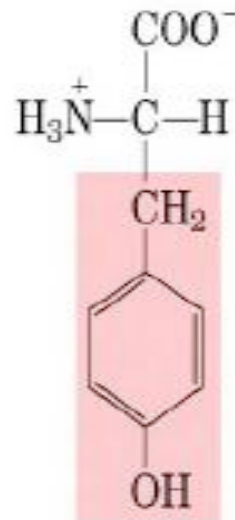
1. Introduction

1. Amino Acids

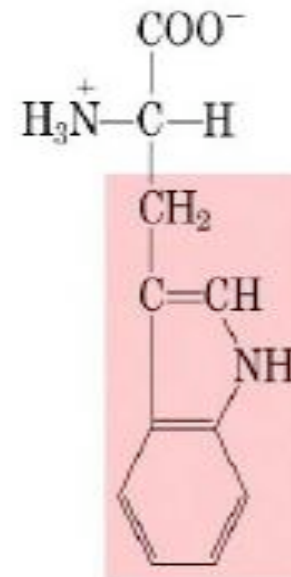
Aromatic R groups



Phenylalanine



Tyrosine

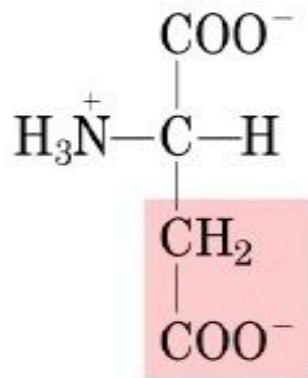


Tryptophan

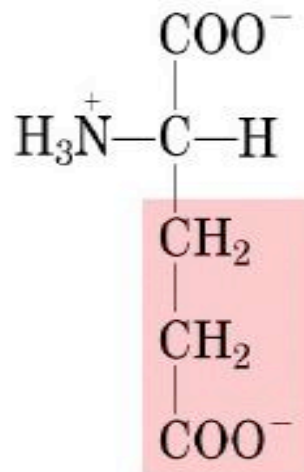
1. Introduction

1. Amino Acids

Negatively charged R groups

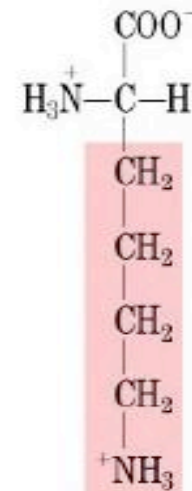


Aspartate

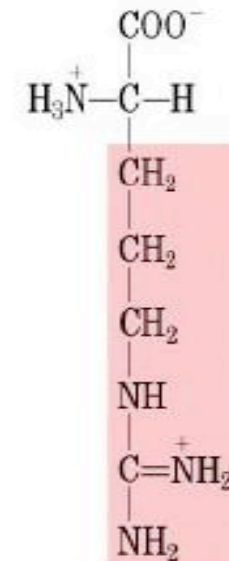


Glutamate

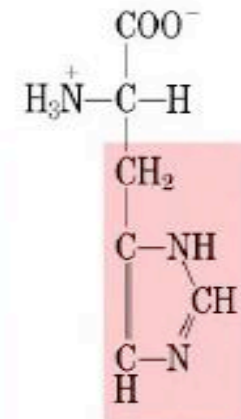
Positively charged R groups



Lysine



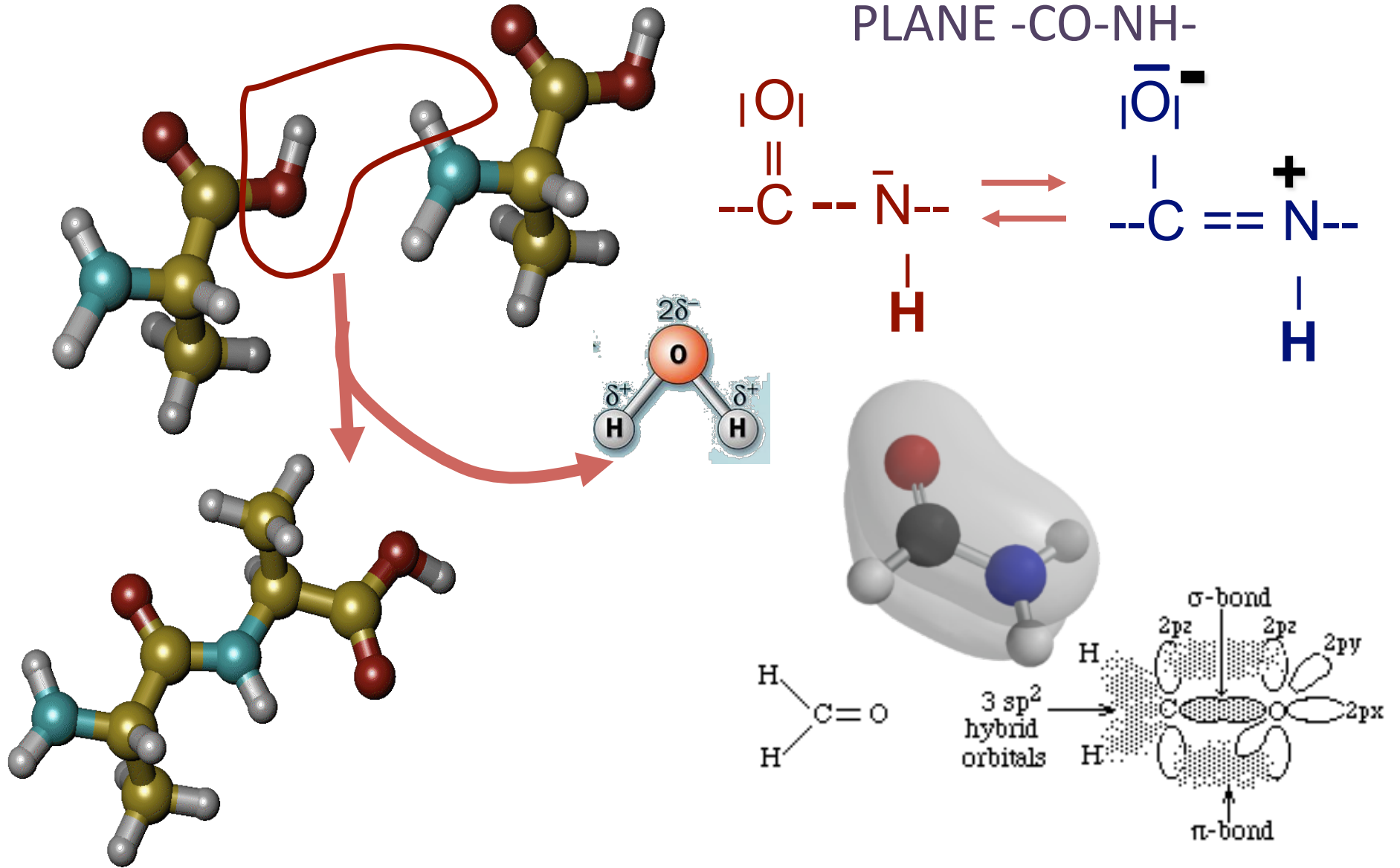
Arginine



Histidine

1. Introduction

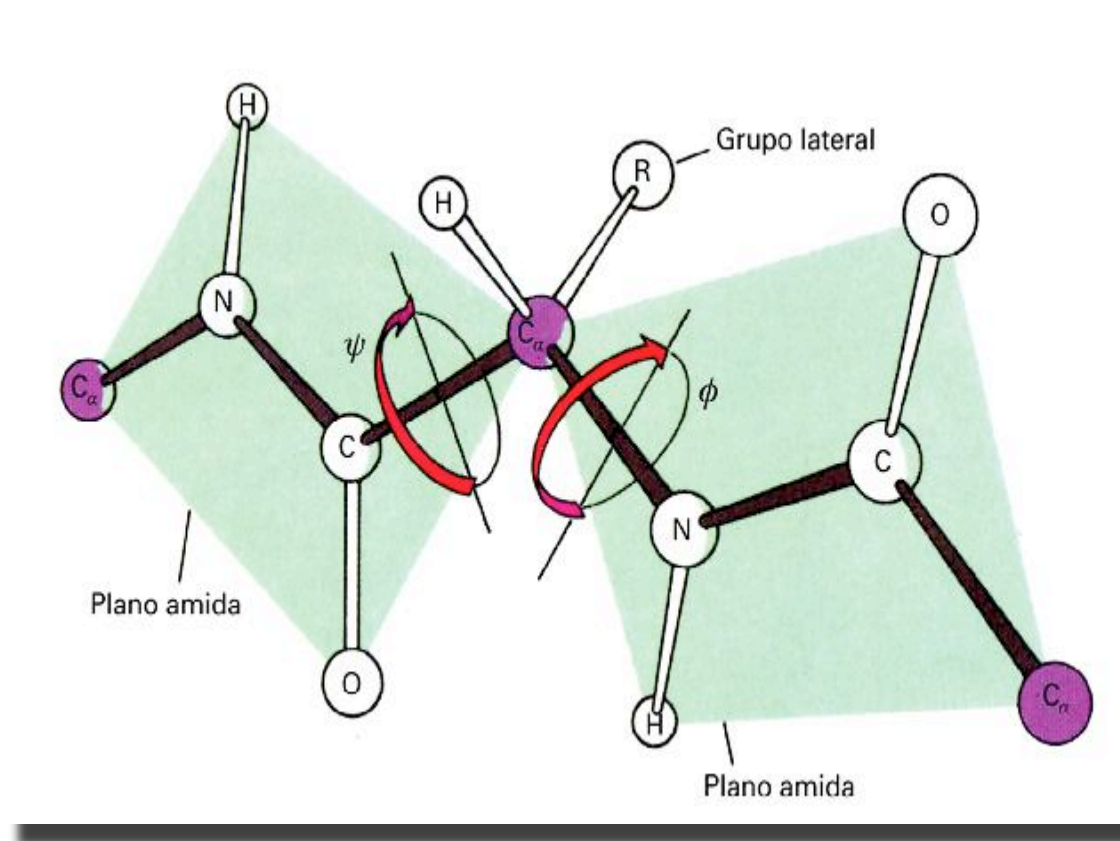
2. Peptide Bond



1. Introduction

2. Peptide Bond

Angles ϕ & ψ



$$\psi = [-180^\circ, +180^\circ]$$

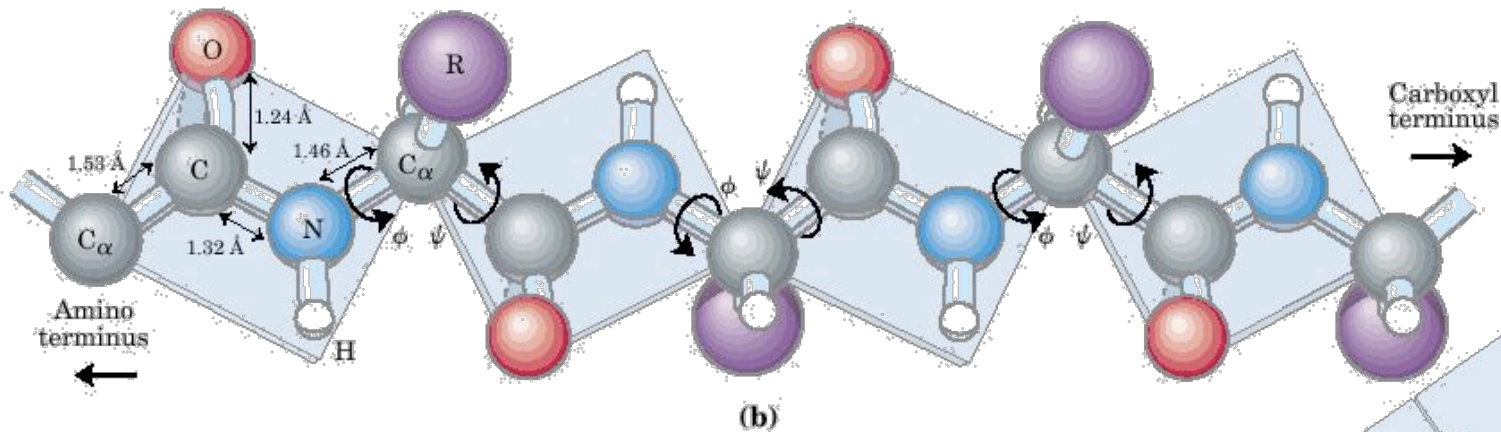
$$\phi = [-180^\circ, +180^\circ]$$

1. Introduction

3. Native Conformation

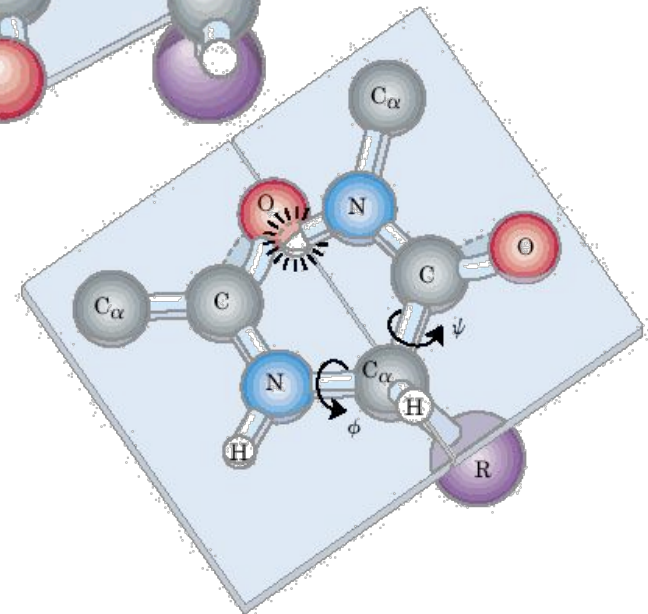
Native conformation:

- 1) Polipeptide + environment
- 2) Function & stability



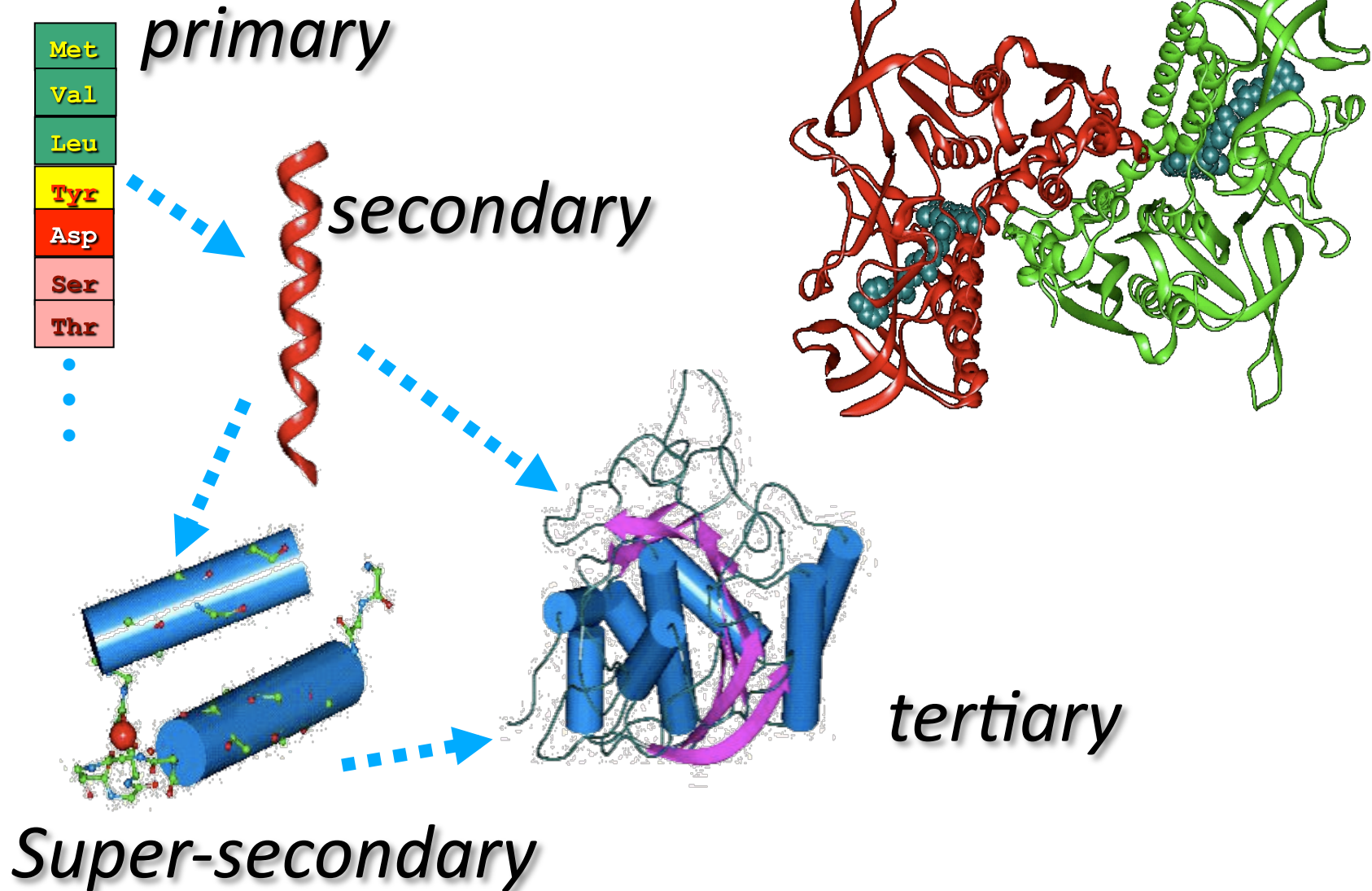
Conformational restraints:

- 1) Peptide bond planarity
- 2) The total space is not 360×360



1. Introduction

4. Levels of structure



2. Energy

1. Bonding energy terms

$$\vec{F} = m * \vec{a} = \sum_{i=1}^N \vec{F}_i$$

$$W = \int_{path} \vec{F} * d\vec{r}$$

2. Energy

1. Bonding energy terms

$$\vec{a} = \frac{\partial}{\partial t} \left(\frac{\partial \vec{r}}{\partial t} \right) = \frac{\partial \vec{v}}{\partial t}$$

$$d\vec{r} = \vec{v} * dt$$

$$\frac{\partial(v^2)}{\partial t} = \frac{\partial(\vec{v} * \vec{v})}{\partial t} = 2 \left(\vec{v} * \frac{\partial \vec{v}}{\partial t} \right)$$

$$\vec{F} * d\vec{r} = \left(m * \frac{\partial \vec{v}}{\partial t} \right) * (\vec{v} * dt) = \frac{1}{2} m \frac{\partial(v^2)}{\partial t} dt$$

2. Energy

1. Bonding energy terms

$$W = \int_{Path} \vec{F} * d\vec{r} = \int_{Time} \frac{1}{2} m \frac{\partial(v^2)}{\partial t} dt = \frac{1}{2} mv^2 + C$$

$$Potential = E_p = - \int_{Path} \vec{F} * d\vec{r}$$

$$Kinetic = E_k = \frac{1}{2} mv^2$$

$$Total = U = E_p + E_k$$

2. Energy

1. Bonding energy terms

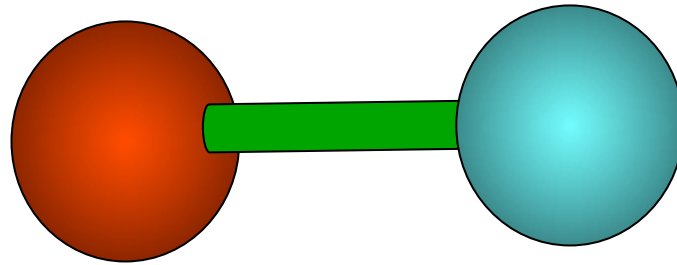
Molecular mechanics

$$\begin{aligned} V = & \frac{1}{2} \sum_i K_i^{bond} (d_i - d_{0,i})^2 + \frac{1}{2} \sum_i K_i^{angle} (\alpha_i - \alpha_{0,i})^2 + \frac{1}{2} \sum_i K_i^{dihedral} (\omega_i - \omega_{0,i})^2 \\ & + \frac{1}{2} \sum_i K_i^{torsion} \cos(\lambda_i \phi_i + \delta_i) + \frac{1}{4\pi\epsilon} \sum_i \sum_{j>i} \frac{q_i q_j}{r_{ij}} + \sum_i \sum_{j>i} \left(\frac{C_6(i,j)}{r_{ij}^6} - \frac{C_{12}(i,j)}{r_{ij}^{12}} \right) \\ & + \sum_i (Hydrogen - Bonds) + \sum_i (\pi - \pi) \end{aligned}$$

2. Energy

1. Bonding energy terms

Bond



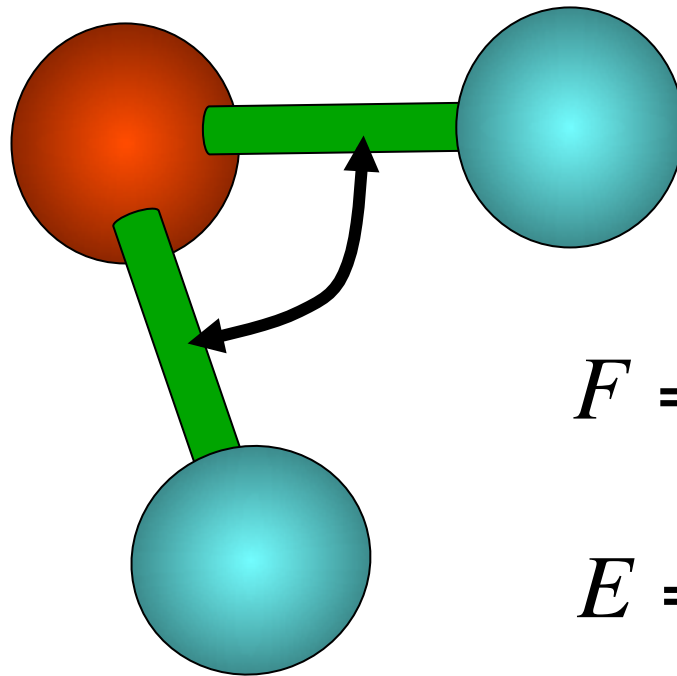
$$F = -k(d - d_0)$$

$$E = \frac{1}{2}k(d - d_0)^2$$

2. Energy

1. Bonding energy terms

Angle



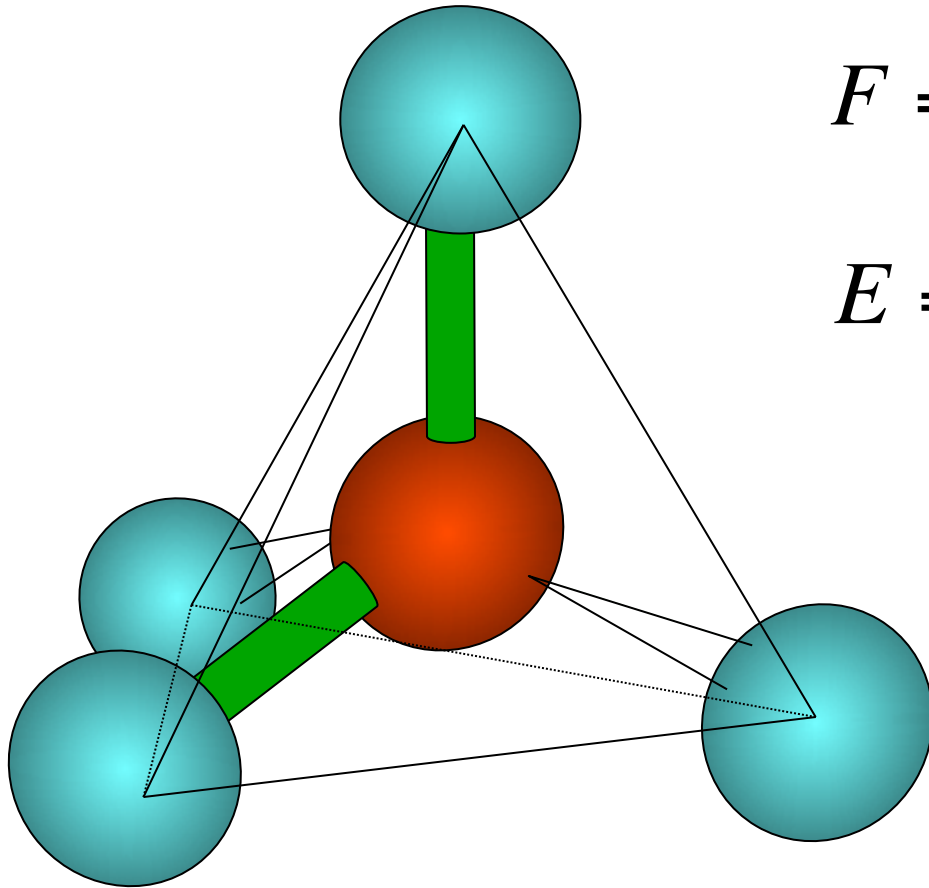
$$F = -k(\alpha - \alpha_0)$$

$$E = \frac{1}{2}k(\alpha - \alpha_0)^2$$

2. Energy

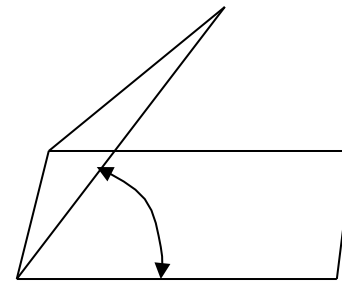
1. Bonding energy terms

Improper dihedral



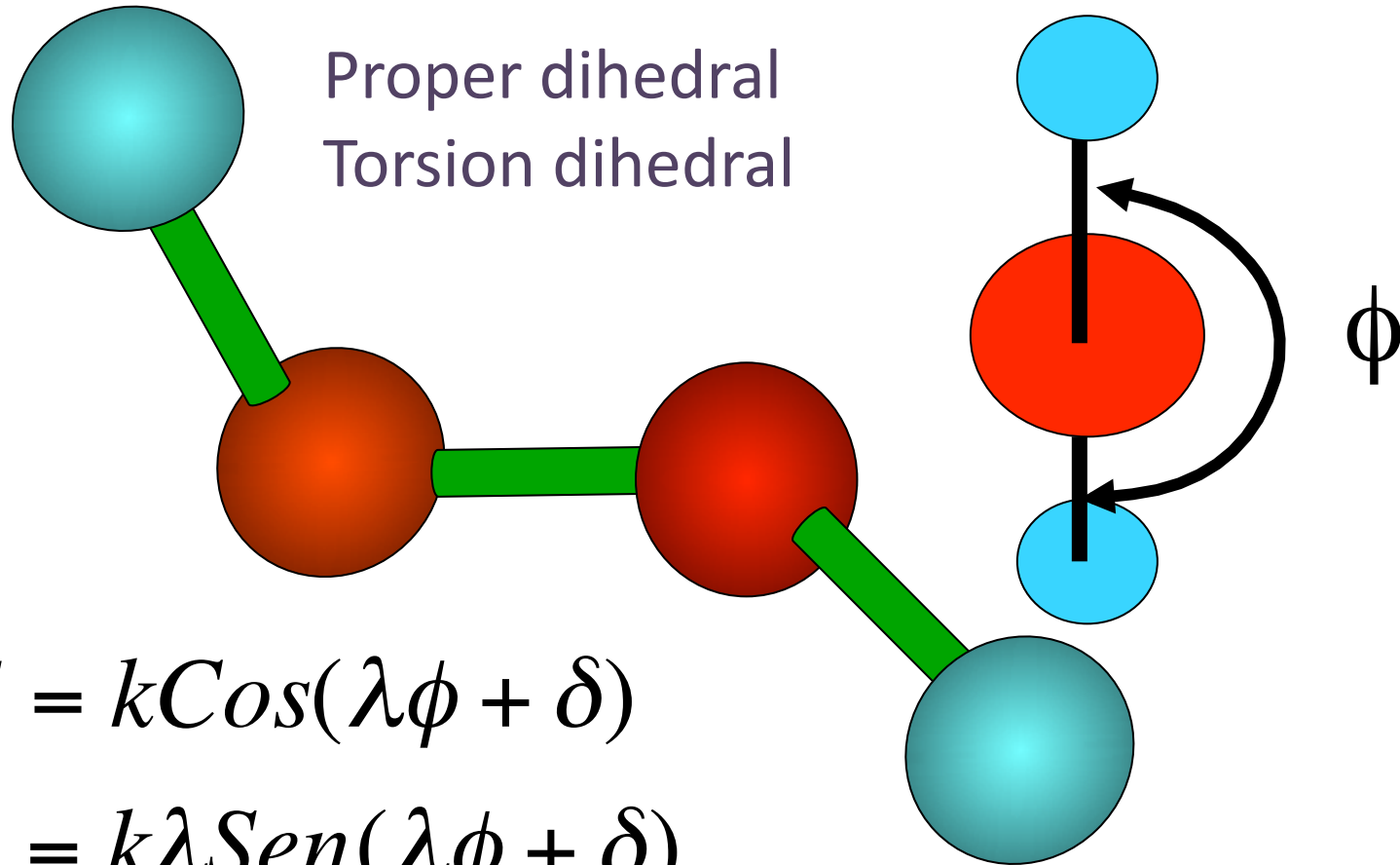
$$F = -k(\varpi - \varpi_0)$$

$$E = \frac{1}{2} k(\varpi - \varpi_0)^2$$



2. Energy

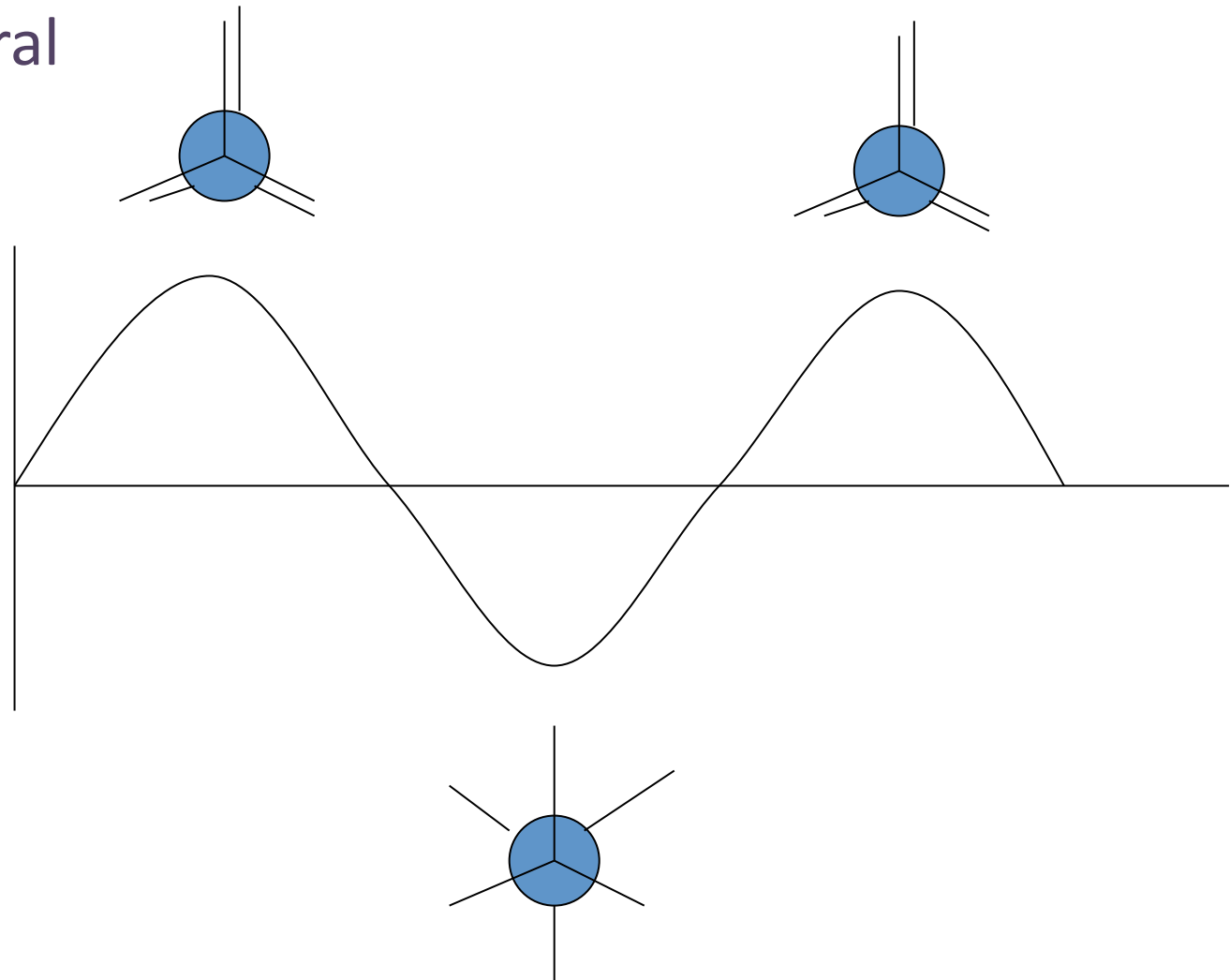
1. Bonding energy terms



2. Energy

1. Bonding energy terms

Proper dihedral
Torsion dihedral



2. Energy

2. Non-Bonding terms

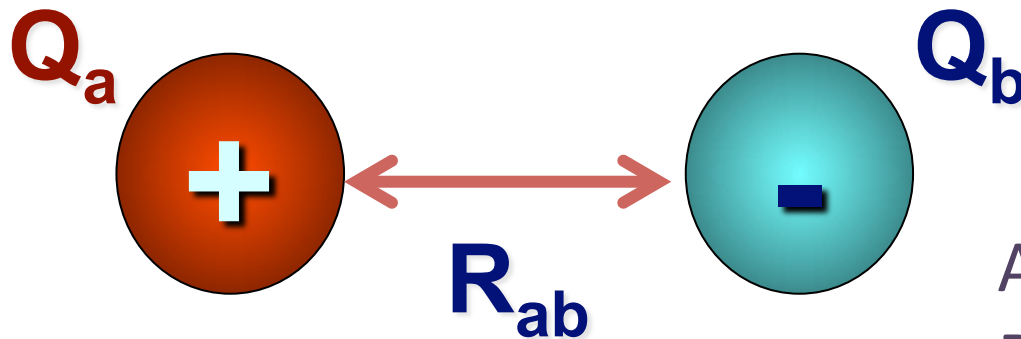
Electrostatic energy

Long range interactions

Involve in folding

$$\vec{F} = -\frac{1}{4\pi\epsilon_0} \frac{Q_a Q_b}{r_{ab}^2} \left(\frac{\vec{r}_{ab}}{r_{ab}} \right)$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q_a Q_b}{r_{ab}}$$



Attraction: opposite sign

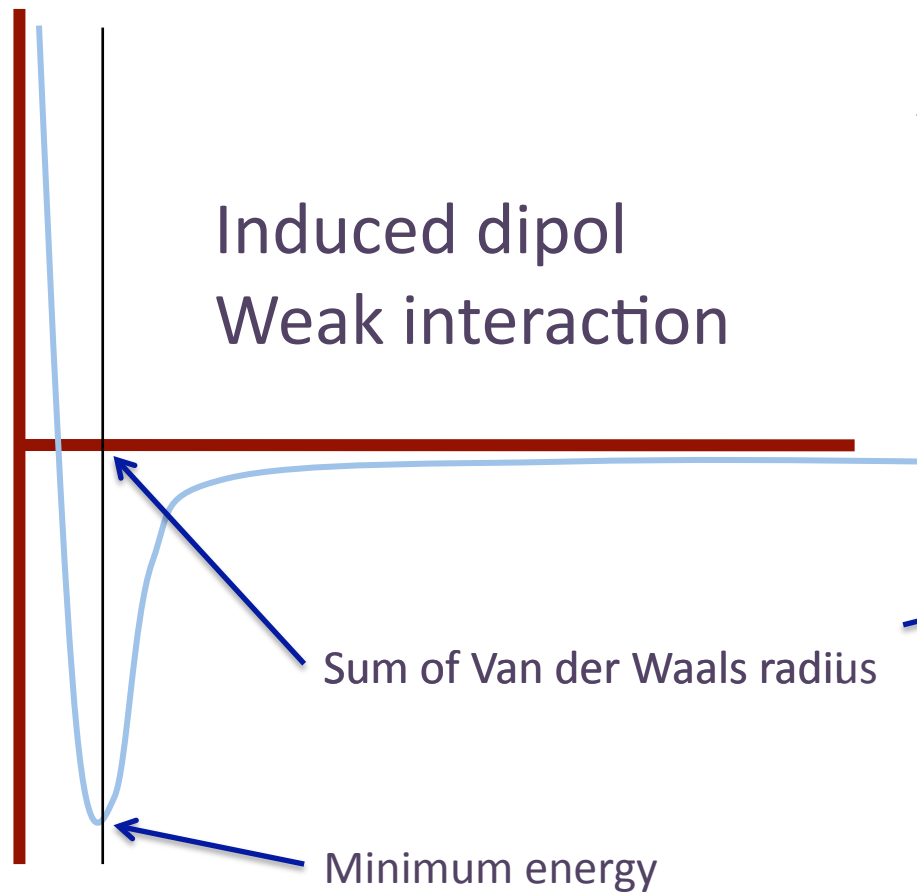
Repulsion: same sign

Approx. 150 kcal/mol

2. Energy

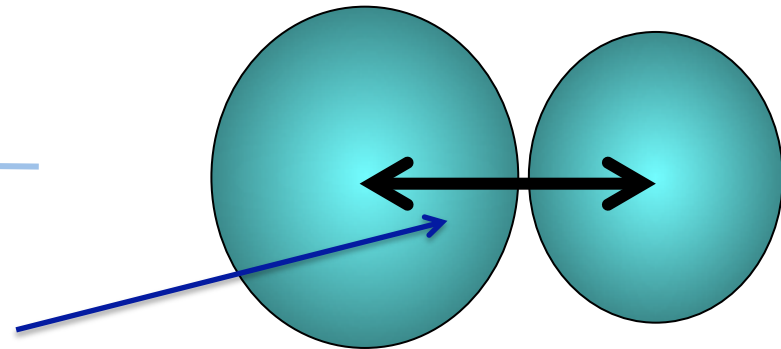
2. Non-Bonding terms

Van der Waals energy



Lennard-Jones equation

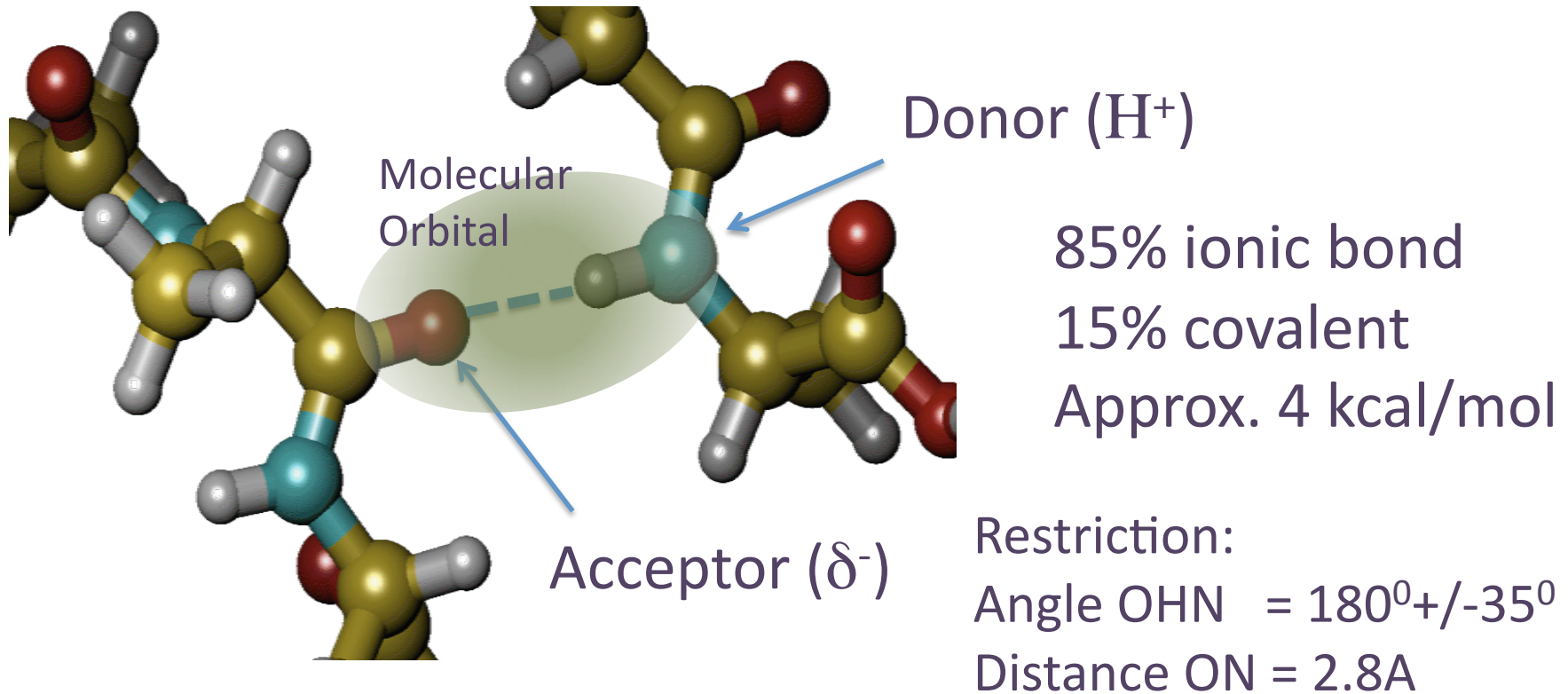
$$E = \frac{C_6(a,b)}{r_{ab}^6} - \frac{C_{12}(a,b)}{r_{ab}^{12}}$$



Avoids atoms collision
Approx. 2 kcal/mol

2. Energy

3. Hydrogen Bonds

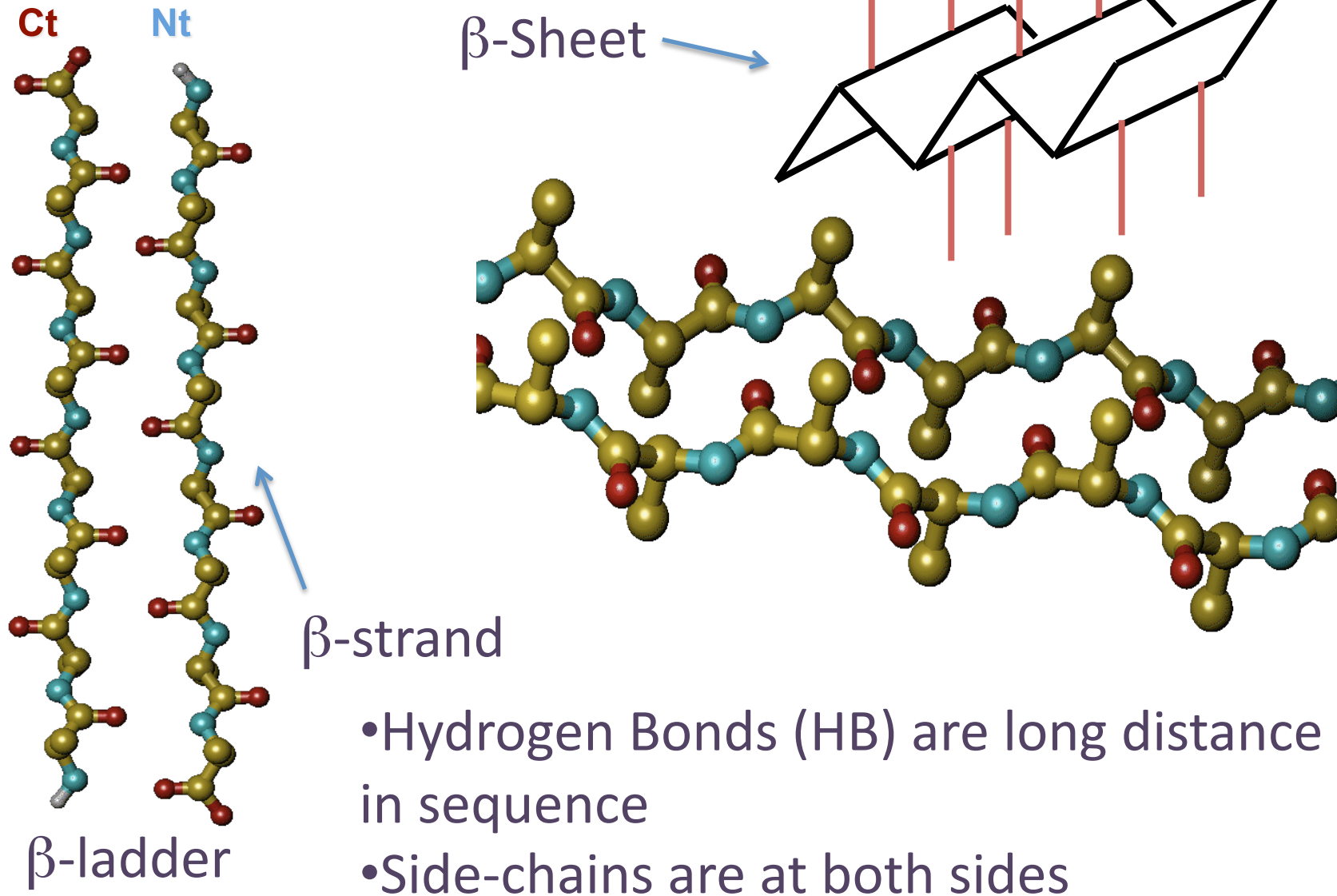


Inter-chain (long distance/short distance in sequence)

Intra-chain

3. Secondary Structure

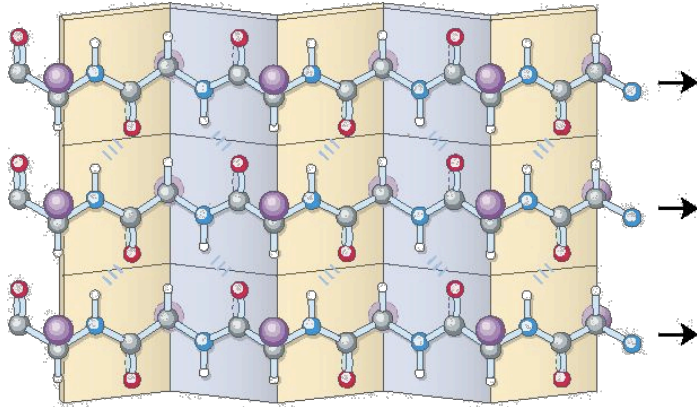
1. Strands



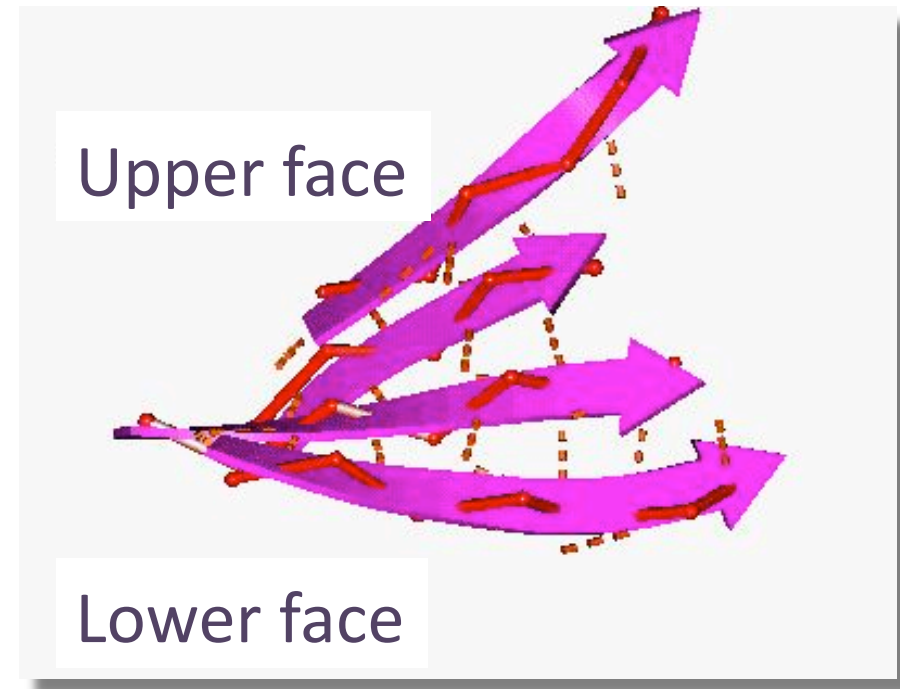
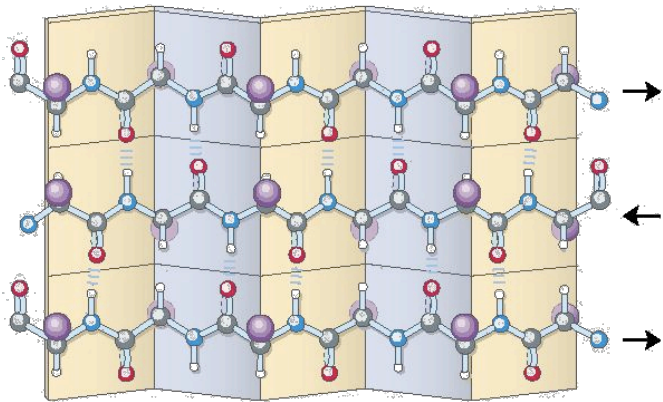
3. Secondary Structure

1. Strands

Parallel β -sheet

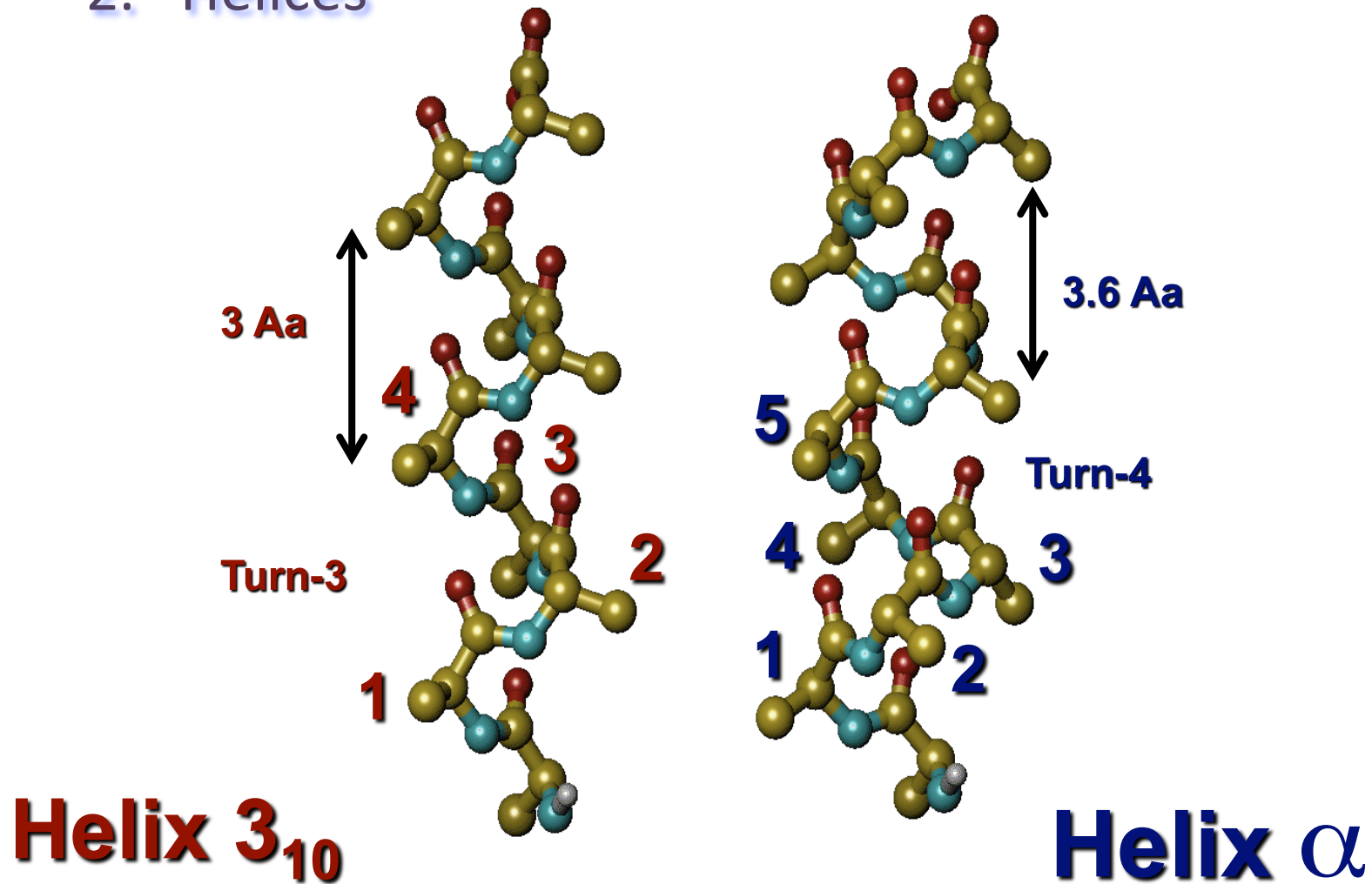


Anti-parallel β -sheet



3. Secondary Structure

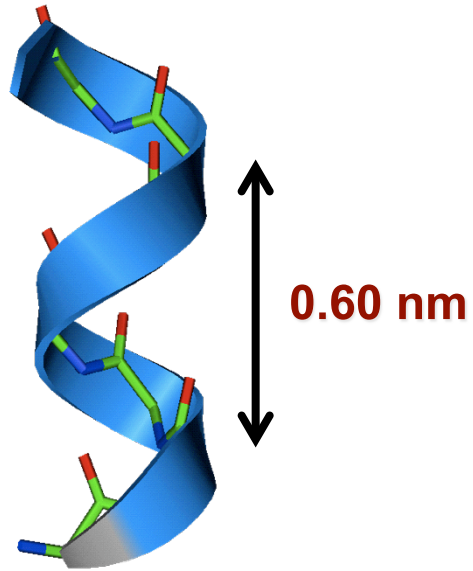
2. Helices



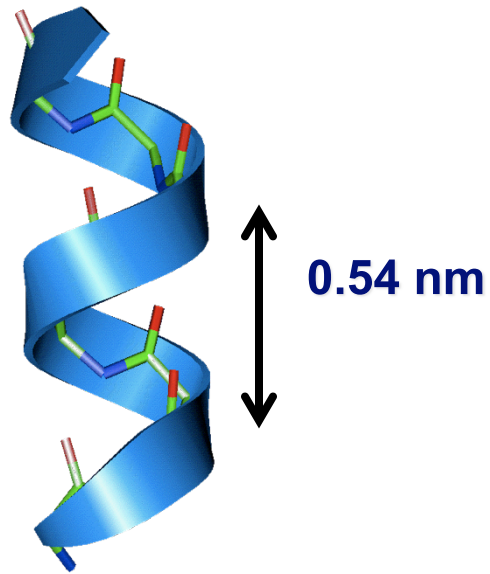
- HB are short distance in sequence
- Side-chains protrude out of the helix

3. Secondary Structure

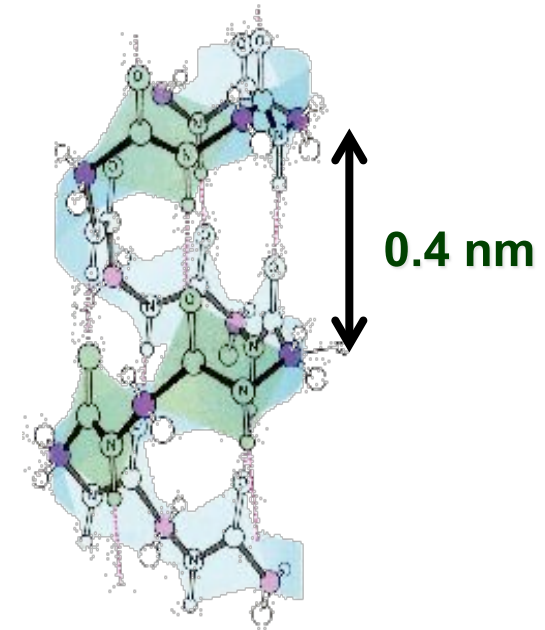
2. Helices



Helix 3₁₀



Helix α

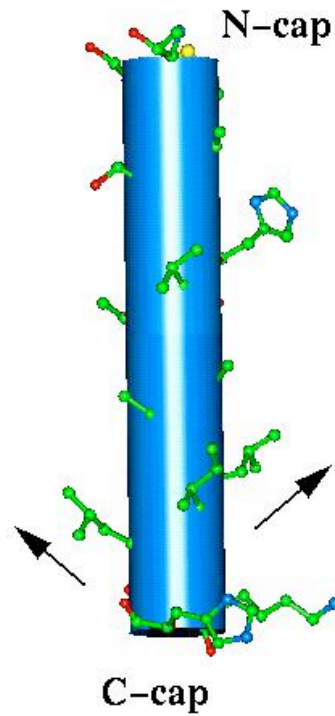
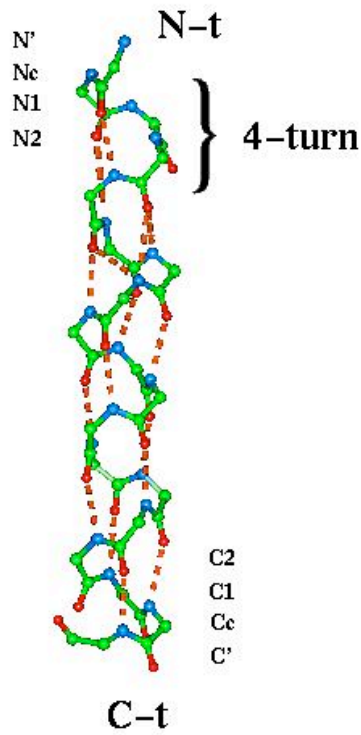


Helix π

UNSTABLE

3. Secondary Structure

2. Helices



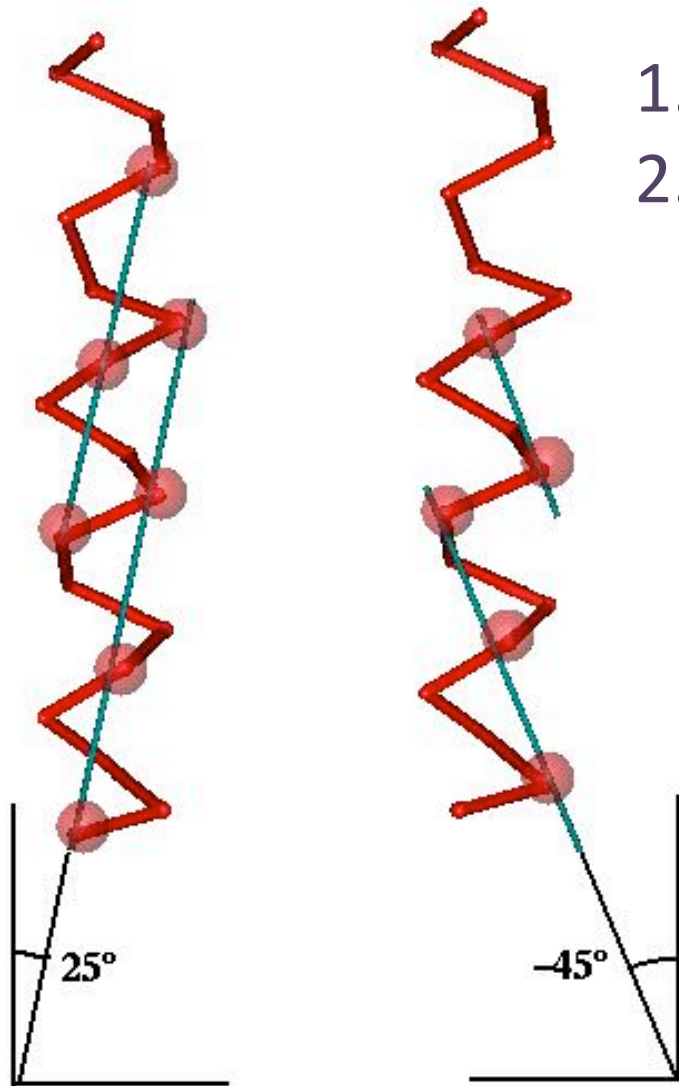
	Hbond	Hydrofobic
N-cap box	N_c-N_3	$N'-N_4$
Big box	N_c-N_3	$N''-N_4$
Shellman	$C''-C_3$ $C'-C_2$	$C''-C_3$
α_L	$C'-C_3$	$C''-C_3$

3. Secondary Structure

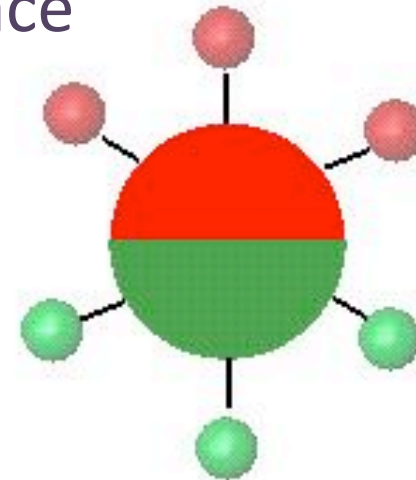
2. Helices

Side-chains location in the helix:

1. Groove formation as in a screw
2. Amphipathic helix: two faces with different solvation properties



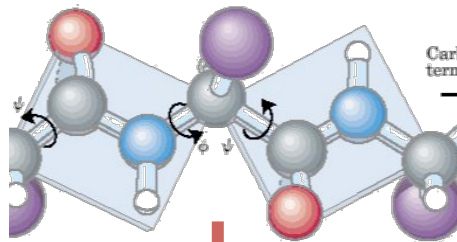
Polar face



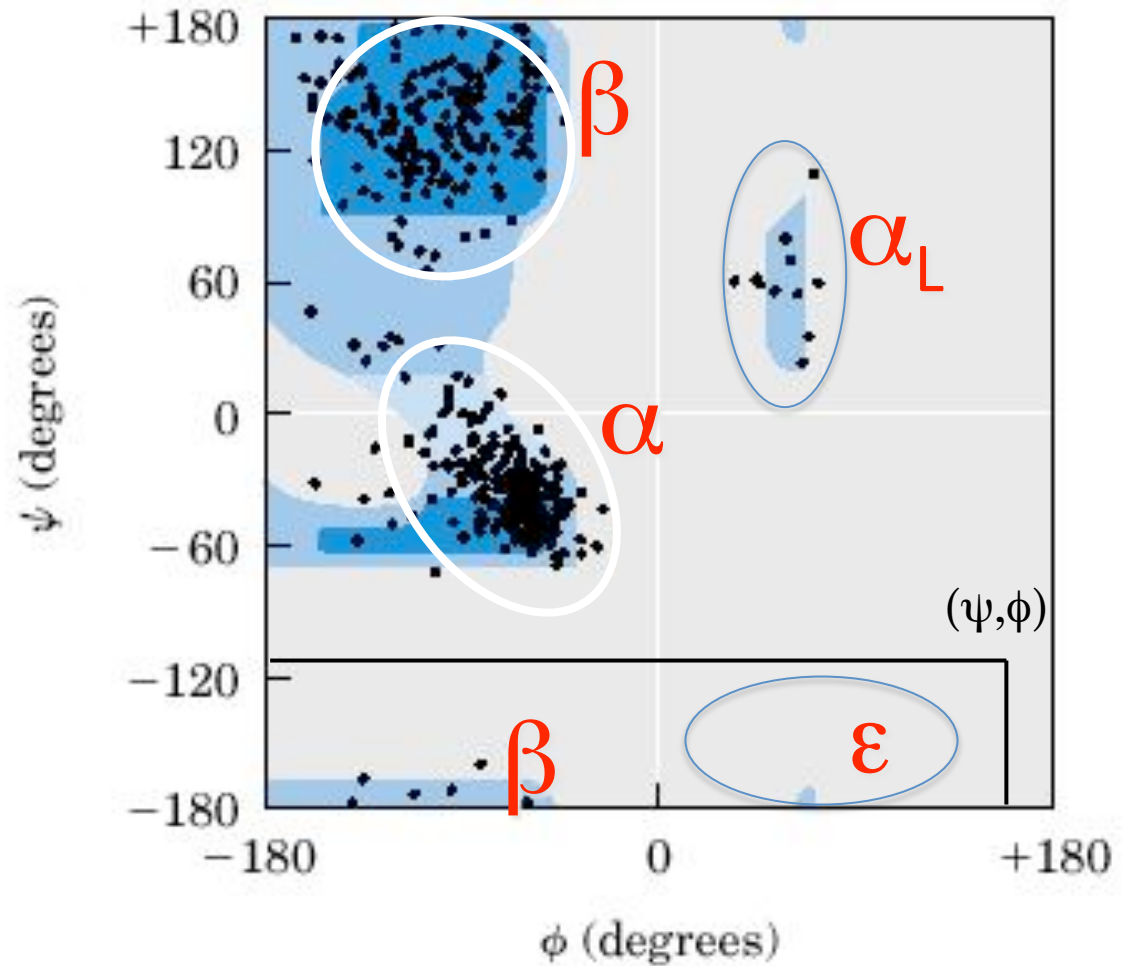
Non-polar face
(hydrophobic)

3. Secondary Structure

3. Ramachandran Plot



(ψ, ϕ)



3. Secondary Structure

4. Aa propensity

